

# DO NOW

Pick up Classwork 4.6.  
Complete the front side.

## 4.6 Summary of Curve Sketching

Methods to analyze the graph of a function include:

x-intercepts	domain and range
y-intercepts	symmetry
continuity	differentiability
vertical asymptotes	horizontal asymptotes
relative extrema	increasing/decreasing
points of inflection	concavity
infinite limits at infinity	

### Procedure:

- Find first and second derivatives.
- Identify the x and y-intercepts, domain, symmetry, horizontal and vertical asymptotes.

X-intercepts  $\rightarrow y=0$ , solve for x  
 Y-intercepts  $\rightarrow x=0$ , solve for y  
 domain  $\rightarrow$  watch for denom=0 or  $\sqrt{\text{negatives}}$   
 Vertical asymptotes  $\rightarrow$  denom=0  
 horizontal asymptotes  $\rightarrow \lim_{x \rightarrow \infty}$  or  $\lim_{x \rightarrow -\infty}$   
 Symmetry: x-axis:  $-f(x)=f(x)$  or replace y with -y  
 y-axis:  $f(x)=f(-x)$  or replace x with -x  
 Origin:  $-f(x)=f(x)$  or place x and y with -x and -y

### Back side of Worksheet CW 4.6

9.  $f(x) = \frac{x}{x^2-9}$

X-intercepts:  $(0, 0)$   
 Y-intercepts:  $(0, 0)$   
 domain:  $(-\infty, -3) \cup (-3, 3) \cup (3, \infty)$   
 Vertical asymptotes:  $x=-3$  and  $x=3$   
 horizontal asymptotes:  $y=0$   
 Symmetry: x-axis: no  
 y-axis: no  
 origin: yes

10.  $f(x) = \frac{2x+1}{3x}$

X-intercept:  $(-\frac{1}{2}, 0)$   
 Y-intercept: none  
 domain:  $(-\infty, 0) \cup (0, \infty)$   
 Vertical asymptotes:  $x=0$   
 horizontal asymptotes:  $y=\frac{2}{3}$   
 Symmetry: x-axis: no  
 y-axis: no  
 origin: no

- Identify the critical numbers and possible points of inflection.

Critical #'s  
 $\hookrightarrow$  1<sup>st</sup> derivative is zero or undefined  
 possible points of inflections  
 $\hookrightarrow$  2<sup>nd</sup> derivative is zero or undefined

On HW worksheet:

- Find 1<sup>st</sup> and 2<sup>nd</sup> derivatives
- Identify x-intercepts etc.
- Find critical #'s and possible points of inflections

# **HOMEWORK**

pg 255 - 256; 1 - 4  
Worksheet HW 4.6